

EXAMEN DU SEMESTRE HARMATTANEPREUVE : MTH2121DURÉE : 2H00Exercice 1

By the Laplace transform method, solve

$$1. \begin{cases} u_t = u_{xx} - hu, & 0 < x < \pi, t > 0 \\ u(x, 0) = \sin x, & 0 \leq x \leq \pi \\ u(0, t) = u(\pi, t) = 0, & t > 0 \end{cases}$$

$$2. \begin{cases} u_{tt} = u_{xx} + h, & 0 < x < \pi, t > 0 \\ u(x, 0) = u_t(x, 0) = 0, & 0 \leq x \leq \pi \\ u_x(0, t) = u_x(\pi, t) = 0, & t > 0 \end{cases}$$

Exercice 2

By the separation of variable method, solve the radioactive decay problem :

$$\begin{cases} u_t - ku_{xx} = Ae^{-ax}, & 0 < x < \pi, t > 0 \\ u(x, 0) = \sin x, & 0 < x < \pi, \\ u(0, t) = u(\pi, t) = 0, & t > 0 \end{cases}$$

where  $A, k$  and  $a$  are the constants.